

TRIGONOMETRIC RATIOS

1) Which of the following is not defined?
 (a) $\cos 0^\circ$ (b) $\tan 45^\circ$ (c) $\sec 90^\circ$ (d) $\sin 90^\circ$

ans: $\cos 90^\circ = 0$
 $\sec 90^\circ = \text{not defined (c)}$

2) The maximum value of $\frac{1}{\operatorname{cosec} \theta}$ ($0^\circ \leq \theta \leq 90^\circ$) is

(a) 1 (b) 0 (c) $\frac{1}{2}$ (d) $\frac{\sqrt{3}}{2}$

ans: $\frac{1}{\operatorname{cosec} \theta} = \sin \theta$

θ	0°	30°	45°	60°	90°
	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1

\therefore maximum value is 1 (a)

3) If $\tan A = \frac{3}{4}$ and A is acute, then the value of $\cos A$ is

(a) $\frac{5}{4}$ (b) $\frac{5}{3}$ (c) $\frac{3}{5}$ (d) $\frac{4}{5}$

ans: $\tan A = \frac{3}{4}$

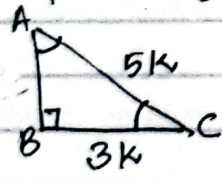
$$\sec^2 A = 1 + \tan^2 A = 1 + \frac{9}{16} = \frac{25}{16} \Rightarrow \sec A = \frac{5}{4}$$

$$\therefore \cos A = \frac{1}{\sec A} = \frac{4}{5} \text{ (d)}$$

4) In $\triangle ABC$, if $\angle B = 90^\circ$, $\sin A = \frac{3}{5}$, then the value of $\cos C$ is

(a) $\frac{5}{4}$ (b) $\frac{4}{5}$ (c) $\frac{3}{5}$ (d) $\frac{5}{3}$

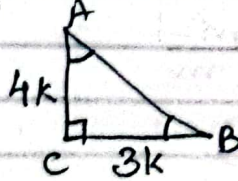
ans:



$$\cos C = \frac{BC}{AC} = \frac{4k}{5k} = \frac{4}{5} \text{ (b)}$$

5) In $\triangle ABC$, if $\angle A + \angle B = 90^\circ$, $\cot B = \frac{3}{4}$, then the value of $\tan A$ is (a) $\frac{4}{5}$ (b) $\frac{3}{4}$ (c) $\frac{4}{3}$ (d) $\frac{3}{5}$

ans:

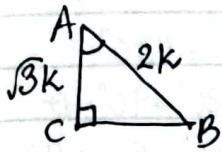


$$\tan A = \frac{BC}{AC} = \frac{3k}{4k} = \frac{3}{4} \text{ (b)}$$

6) If $\sec A = \frac{2}{\sqrt{3}}$ and $\angle A + \angle B = 90^\circ$, then the value of $\operatorname{cosec} B$ is

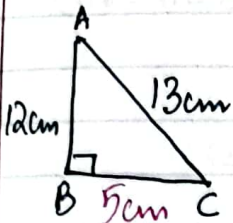
- (a) $\frac{1}{\sqrt{3}}$ (b) $\frac{\sqrt{3}}{2}$ (c) $\frac{2}{\sqrt{3}}$ (d) $\sqrt{3}$

ans:-



$$\operatorname{cosec} B = \frac{AB}{AC} = \frac{2k}{\sqrt{3}k} = \frac{2}{\sqrt{3}} \text{ (c)}$$

7)



$\tan A - \cot C$ is equal to

- (a) $\frac{7}{13}$ (b) $-\frac{7}{13}$ (c) $\frac{5}{12}$ (d) 0

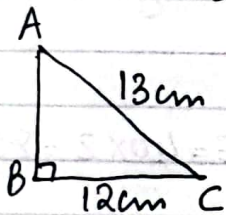
ans:-

Using Pythagoras Theorem in $\triangle ABC$, $BC^2 = AC^2 - AB^2$
 $= 13^2 - 12^2$
 $= 169 - 144 = 25$
 $BC = 5 \text{ cm}$

$$\tan A = \frac{BC}{AB} = \frac{5}{12} ; \cot C = \frac{BC}{AB} = \frac{5}{12}$$

$$\therefore \tan A - \cot C = \frac{5}{12} - \frac{5}{12} = 0 \text{ (d)}$$

8)

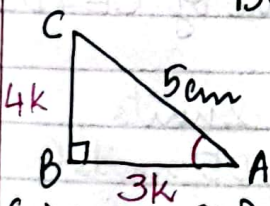


In the figure, $AC = 13 \text{ cm}$, $BC = 12 \text{ cm}$, then $\sec C$ is equal to (a) $\frac{13}{12}$ (b) $\frac{5}{12}$ (c) $\frac{12}{13}$ (d) $\frac{5}{13}$

ans:-

$$\sec C = \frac{AC}{BC} = \frac{13}{12} \text{ (a)}$$

9)



In the given figure, $\triangle ABC$ is right-angled at B and $\tan A = \frac{4}{3}$. If $AC = 5 \text{ cm}$, the length of BC is

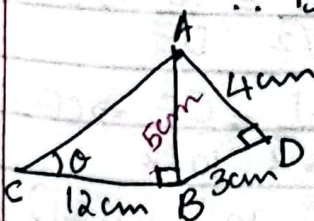
- (a) 4cm (b) 3cm (c) 12cm (d) 9cm

ans:-

$$\tan A = \frac{BC}{AB} = \frac{4k}{3k} = \frac{4}{3} ; k = 1$$

$$\therefore BC = 4 \text{ cm (a)}$$

10)



In the given figure, $AD = 4 \text{ cm}$, $BD = 3 \text{ cm}$ and $CB = 12 \text{ cm}$, the value of $\cot \theta$ is

- (a) $\frac{12}{5}$ (b) $\frac{5}{12}$ (c) $\frac{13}{12}$ (d) $\frac{12}{13}$

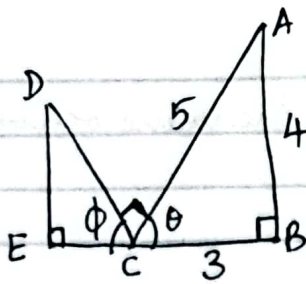
ans:-

In rt. $\triangle ABD$, $AB^2 = AD^2 + BD^2 = 4^2 + 3^2 = 16 + 9 = 25$

$$AB = 5 \text{ cm}$$

$$\therefore \cot \theta = \frac{BC}{AB} = \frac{12}{5} \text{ (a)}$$

11)



In the given figure, the value of $\cos \phi$ is (a) $\frac{5}{4}$ (b) $\frac{5}{3}$ (c) $\frac{3}{5}$ (d) $\frac{4}{5}$

Ans:

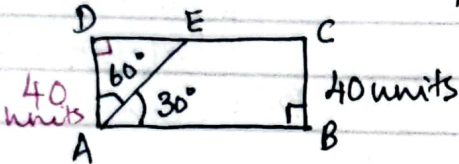
Since ECB is a straight line, $\phi + 90^\circ + \theta = 180^\circ$
 $\Rightarrow \phi = 180^\circ - 90^\circ - \theta$
 $\Rightarrow \phi = 90^\circ - \theta \rightarrow (1)$

In rt. $\triangle ABC$, $\angle A + \theta + 90^\circ = 180^\circ$
 $\Rightarrow \angle A = 180^\circ - 90^\circ - \theta$
 $\Rightarrow \angle A = 90^\circ - \theta \rightarrow (2)$

From (1) and (2), $\phi = \angle A$

$$\therefore \cos \phi = \cos A = \frac{AB}{AC} = \frac{4}{5} \text{ (d)}$$

12)



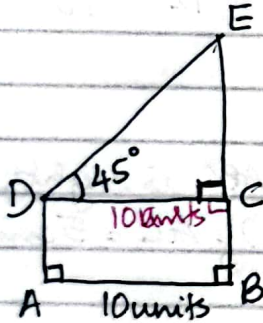
If ABCD is a rectangle, then AE is equal to
 (a) 80 units (b) 90 units
 (c) 85 units (d) 70 units.

Ans: $BC = AD = 40$ units (opposite sides of rectangle ABCD)

In $\triangle ADE$, $\cos A = \frac{AD}{AE} \Rightarrow \cos 60^\circ = \frac{40}{AE}$

$$\Rightarrow \frac{1}{2} = \frac{40}{AE} \Rightarrow AE = 40 \times 2 = 80 \text{ units (a)}$$

13)



In the figure, the value of $CE + DE$ (using $\sqrt{2} = 1.41$) is

(a) 36.15 units (b) 48.2 units
 (c) 24.1 units (d) 12.05 units

Ans:

In rectangle ABCD, $AB = CD = 10$ units

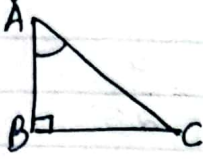
In rt. $\triangle DCE$, $\cos 45^\circ = \frac{DC}{DE} \Rightarrow \frac{1}{\sqrt{2}} = \frac{10}{DE} \Rightarrow DE = 10\sqrt{2}$ units

$$\sin 45^\circ = \frac{CE}{DE} \Rightarrow \frac{1}{\sqrt{2}} = \frac{CE}{10\sqrt{2}} \Rightarrow CE = 10 \text{ units}$$

$$\therefore CE + DE = 10 + 10\sqrt{2} = 10(1 + \sqrt{2}) = 10(1 + 1.41) = 10 \times 2.41 = 24.1 \text{ units (c)}$$

- 14) If A is an acute angle in a right $\triangle ABC$, right-angled at B , then the value of $\sin A + \cos A$ is
 (a) equal to 1 (b) greater than 1 (c) less than 1 (d) 2

ans:-



$$\sin A + \cos A = \frac{BC}{AC} + \frac{AB}{AC} = \frac{BC+AB}{AC}$$

Since $BC+AB > AC$, $\sin A + \cos A > 1$ (b)

- 15) If $\cos \theta = \frac{1}{2}$, then the value of $\cos \theta - \sec \theta$ is

(a) $\frac{3}{2}$ (b) $-\frac{3}{2}$ (c) $\frac{\sqrt{3}}{2}$ (d) $-\frac{\sqrt{3}}{2}$

ans:- $\cos \theta = \frac{1}{2} \Rightarrow \theta = 60^\circ$

$$\therefore \cos 60^\circ - \sec 60^\circ = \frac{1}{2} - 2 = \frac{1-4}{2} = -\frac{3}{2} \text{ (b)}$$

- 16) If $\cot A = \frac{12}{5}$, then the value of $(\sin A + \cos A) \times \operatorname{cosec} A$ is

(a) $\frac{13}{5}$ (b) $\frac{17}{5}$ (c) $\frac{14}{5}$ (d) 1

ans:- $(\sin A + \cos A) \operatorname{cosec} A = \sin A \cdot \operatorname{cosec} A + \cos A \cdot \operatorname{cosec} A$

$$= \frac{\sin A}{\sin A} + \frac{\cos A}{\sin A}$$

$$= \cot A + 1 = \frac{12}{5} + 1 = \frac{12+5}{5} = \frac{17}{5} \text{ (b)}$$

- 17) If $\operatorname{cosec} A = 2$, then the value of $\cot A + \frac{\sin A}{1+\cos A}$ is

(a) $\frac{2}{3}$ (b) $\frac{3}{2}$ (c) 2 (d) $\frac{1}{2}$

ans:- $\cot A + \frac{\sin A}{1+\cos A} = \frac{\cos A}{\sin A} + \frac{\sin A}{1+\cos A} = \frac{\cos A(1+\cos A) + \sin^2 A}{\sin A(1+\cos A)}$

$$= \frac{\cos A + (\cos^2 A + \sin^2 A)}{\sin A(1+\cos A)}$$

$$= \frac{\cos A + 1}{\sin A(1+\cos A)} = \frac{1}{\sin A} = \operatorname{cosec} A = 2 \text{ (c)}$$

18) If $\sec \alpha = \frac{5}{4}$, then the value of $\frac{1 - \tan \alpha}{1 + \tan \alpha}$ is

(a) 2 (b) 7 (c) $\frac{1}{7}$ (d) $\frac{2}{7}$

ans: $\tan^2 \alpha = \sec^2 \alpha - 1 = \frac{25}{16} - 1 = \frac{25-16}{16} = \frac{9}{16}$

$\therefore \tan \alpha = \frac{3}{4}$

Then, $\frac{1 - \tan \alpha}{1 + \tan \alpha} = \frac{1 - \frac{3}{4}}{1 + \frac{3}{4}} = \frac{\frac{4-3}{4}}{\frac{4+3}{4}} = \frac{1}{4} \times \frac{4}{7} = \frac{1}{7}$ (c)

19) If $\sec \theta = \frac{3}{2}$, then $\tan^2 \theta$ is equal to

(a) $\frac{5}{4}$ (b) $\frac{9}{4}$ (c) $\frac{3}{4}$ (d) $\frac{1}{4}$

ans: $\tan^2 \theta = \sec^2 \theta - 1 = \left(\frac{3}{2}\right)^2 - 1 = \frac{9}{4} - 1 = \frac{9-4}{4} = \frac{5}{4}$ (a)

20) If $\cot \theta = \sqrt{5}$, then the value of $\frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta}$ is

(a) $\frac{2}{3}$ (b) $\frac{2}{5}$ (c) $\frac{3}{2}$ (d) $\frac{5}{2}$

ans: $\operatorname{cosec}^2 \theta = 1 + \cot^2 \theta = 1 + 5 = 6$

$\therefore \operatorname{cosec} \theta = \sqrt{6}$

$\Rightarrow \sin \theta = \frac{1}{\sqrt{6}}$

$\therefore \cos^2 \theta = 1 - \sin^2 \theta = 1 - \frac{1}{6} = \frac{6-1}{6} = \frac{5}{6}$

$\Rightarrow \sec^2 \theta = \frac{1}{\cos^2 \theta} = \frac{6}{5} \Rightarrow \sec \theta = \sqrt{\frac{6}{5}}$

$\therefore \frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta} = \frac{6 - \frac{6}{5}}{6 + \frac{6}{5}} = \frac{\frac{30-6}{5}}{\frac{30+6}{5}} = \frac{24}{36}$

$= \frac{2}{3}$ (a)

21) The value of $\frac{\tan 45^\circ}{\sin 30^\circ + \cos 60^\circ}$ is

(a) $\frac{1}{\sqrt{2}}$ (b) 2 (c) $\sqrt{2}$ (d) 1

ans:- $\frac{1}{\frac{1}{2} + \frac{1}{2}} = \frac{1}{1} = 1$ (d)

22) The value of $\operatorname{Cosec} 30^\circ + \cot 45^\circ$ is

(a) -1 (b) 2 (c) 3 (d) 2

ans:- $2 + 1 = 3$ (c)

23) The value of $\sin^2 30^\circ - \cos^2 30^\circ$ is

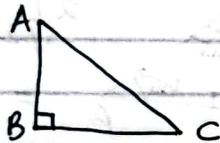
(a) $-\frac{1}{2}$ (b) $\frac{\sqrt{3}}{2}$ (c) $\frac{3}{2}$ (d) $\frac{2}{3}$

ans:- $\left(\frac{1}{2}\right)^2 - \left(\frac{\sqrt{3}}{2}\right)^2 = \frac{1}{4} - \frac{3}{4} = -\frac{2}{4} = -\frac{1}{2}$ (a)

24) In $\triangle ABC$ right angled at B, the value of $\cos(A+C)$ is

(a) $\frac{1}{\sqrt{2}}$ (b) $\frac{1}{2}$ (c) 0 (d) 1

ans:-



Using angle sum property,

$$\angle A + \angle C = 90^\circ$$

$$\cos(A+C) = \cos 90^\circ = 0$$
 (c)

25) If $\theta = 30^\circ$, then the value of $\frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$ is

(a) $\frac{3}{2}$ (b) $\frac{1}{3}$ (c) $\frac{1}{2}$ (d) $\frac{2}{3}$

ans:- $\frac{1 - \left(\frac{1}{\sqrt{3}}\right)^2}{1 + \left(\frac{1}{\sqrt{3}}\right)^2} = \frac{1 - \frac{1}{3}}{1 + \frac{1}{3}} = \frac{\frac{3-1}{3}}{\frac{3+1}{3}} = \frac{2}{4} = \frac{1}{2}$ (c)

26) If $\sin A = \frac{1}{2}$ and $\cos B = \frac{1}{2}$, then the value of $A+B$ is equal to

(a) 0° (b) 60° (c) 90° (d) 30°

ans:- $\sin A = \frac{1}{2} \Rightarrow A = 30^\circ$

$$\cos B = \frac{1}{2} \Rightarrow B = 60^\circ$$

$$\therefore A+B = 30^\circ + 60^\circ = 90^\circ$$
 (c)

27) If $\sin 2A = 1$, $0 < A < 90^\circ$, then the value of A is

(a) 30° (b) 45° (c) 60° (d) 90°

ans:- $\sin 2A = 1 \Rightarrow 2A = 90^\circ$
 $\Rightarrow A = \frac{90^\circ}{2} = 45^\circ$ (b)

28) If $2 \cos 3A = 1$, then the value of A is

(a) 40° (b) 60° (c) 80° (d) 20°

ans:- $2 \cos 3A = 1 \Rightarrow \cos 3A = \frac{1}{2}$
 $\therefore 3A = 60^\circ \Rightarrow A = 20^\circ$ (d)

29) If $\tan 3\theta = \sin 30^\circ + \cos 45^\circ \sin 45^\circ$, then the value of θ is

(a) 15° (b) 30° (c) 45° (d) 60°

ans:- $\tan 3\theta = \frac{1}{2} + \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} = \frac{1}{2} + \frac{1}{2} = 1$
 $\therefore 3\theta = 45^\circ \Rightarrow \theta = \frac{45^\circ}{3} = 15^\circ$ (a)

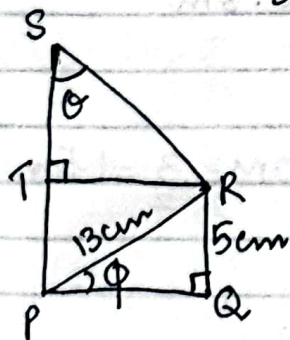
30) If some angle θ , $\cot 2\theta = \frac{1}{\sqrt{3}}$, then the value of $\sin 3\theta$, where $3\theta \leq 90^\circ$ is (a) $\frac{1}{\sqrt{2}}$ (b) 1 (c) 0 (d) $\frac{\sqrt{3}}{2}$

ans:- $\cot 2\theta = \frac{1}{\sqrt{3}} \Rightarrow 2\theta = 60^\circ$ | Then, $\sin 3\theta = \sin 90^\circ = 1$ (b)
 $\therefore \theta = 30^\circ$

31) If $\operatorname{cosec} \theta = 2$, $\cot \theta = \sqrt{3}p$, then the value of p is (a) $\sqrt{3}$ (b) 2 (c) $\frac{2}{\sqrt{3}}$ (d) 1

ans:- $\operatorname{cosec}^2 \theta - \cot^2 \theta = 1$ (or) $\operatorname{cosec} \theta = 2$
 $4 - 3p^2 = 1 \Rightarrow \sin \theta = \frac{1}{2}$
 $4 - 1 = 3p^2 \Rightarrow \therefore \theta = 30^\circ$
 $3p^2 = 3$
 $p^2 = 1 \Rightarrow p = 1$ (d) Then $\cot 30^\circ = \sqrt{3}p$
 $\Rightarrow \sqrt{3} = \sqrt{3}p$
 $\therefore p = 1$

32)



PS = 14 cm, the value of $\tan \theta$ is (a) $\frac{14}{3}$ (b) $\frac{4}{3}$ (c) $\frac{5}{3}$ (d) $\frac{13}{3}$

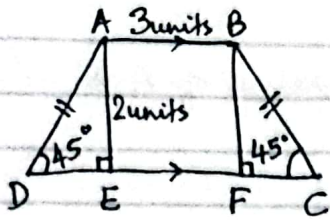
Soln:-

Using Pythagoras Theorem, $PQ^2 = 13^2 - 5^2 = 169 - 25$
 $PQ = \sqrt{144} = 12 \text{ cm}$

Since TPAR is a rectangle, $PQ = TR = 12 \text{ cm}$
 $RQ = TP = 5 \text{ cm}$ | $ST = SP - TP = 14 - 5 = 9 \text{ cm}$

$\therefore \tan \theta = \frac{TR}{ST} = \frac{12}{9} = \frac{4}{3}$ (b)

33)



If ABCD is an isosceles trapezium, its perimeter (using $\sqrt{2} = 1.41$) is
 (a) 17.64 units (b) 18.64 units
 (c) 15.64 units (d) 16.64 units

Ans:-

In rt. $\triangle AED$, $\sin 45^\circ = \frac{AE}{AD}$

$$\Rightarrow \frac{1}{\sqrt{2}} = \frac{2}{AD} \Rightarrow AD = 2\sqrt{2} \text{ units}$$

Also, $\tan 45^\circ = \frac{AE}{DE}$

$$\Rightarrow 1 = \frac{2}{DE} \Rightarrow DE = 2 \text{ units}$$

Thus, $DE = EC = 2$ units

$$AD = BC = 2\sqrt{2} \text{ units}$$

$$AB = EF = 3 \text{ units}$$

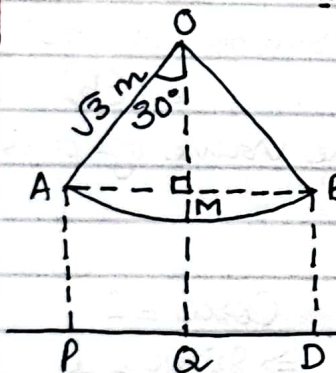
$$\therefore \text{Perimeter} = AB + BC + CD + DA$$

$$= 3 + 2\sqrt{2} + 2 + 3 + 2 + 2\sqrt{2}$$

$$= 10 + 4\sqrt{2} = 10 + 4 \times 1.41 = 10 + 5.64$$

$$= 15.64 \text{ units} // (c)$$

34)



A pendulum of length $\sqrt{3}$ m is attached to a point 2.3 m from the ground. It swings through an angle of 30° on each side of the vertical. The

height above the ground at ends of its path is
 (a) 0.9m (b) 0.6m (c) 0.7m (d) 0.8m

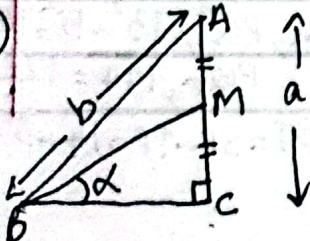
Ans:-

In rt. $\triangle OMA$, $\cos 30^\circ = \frac{OM}{OA}$

$$\Rightarrow \frac{\sqrt{3}}{2} = \frac{OM}{\sqrt{3}} \Rightarrow OM = \frac{3}{2} = 1.5 \text{ m}$$

$$\therefore AP = 2.3 - 1.5 = 0.8 \text{ m} (d)$$

35)



$AM = MC$ and $\angle C$ is a right angle then $\sin^2 \alpha - \cos^2 \alpha = \text{---}$

(a) $\frac{4b^2 - 3a^2}{5a^2 - 4b^2}$ (b) $\frac{5a^2 - 4b^2}{4b^2 - 3a^2}$ (c) $\frac{4a^2 - 5b^2}{3b^2 - 4a^2}$ (d) $\frac{3b^2 - 4a^2}{4a^2 - 5b^2}$

ans:- $AM = MC = \frac{a}{2}$

In rt. $\triangle ABC$, $BC^2 = AB^2 - AC^2 = b^2 - a^2 \rightarrow (1)$

In rt. $\triangle MCB$, $BM^2 = MC^2 + BC^2 = \left(\frac{a}{2}\right)^2 + b^2 - a^2 = \frac{a^2}{4} + b^2 - a^2$

$BM^2 = \frac{a^2 + 4b^2 - 4a^2}{4} = \frac{4b^2 - 3a^2}{4} \rightarrow (2)$

$\sin \alpha = \frac{MC}{BM}$; $\cos \alpha = \frac{BC}{BM}$

$\therefore \sin^2 \alpha - \cos^2 \alpha = \frac{MC^2}{BM^2} - \frac{BC^2}{BM^2} = \frac{MC^2 - BC^2}{BM^2}$
 $= \frac{\left(\frac{a}{2}\right)^2 - b^2 + a^2}{\frac{4b^2 - 3a^2}{4}} = \frac{\frac{a^2}{4} - b^2 + a^2}{\frac{4b^2 - 3a^2}{4}}$
 $= \frac{\frac{a^2 - 4b^2 + 4a^2}{4}}{\frac{4b^2 - 3a^2}{4}} = \frac{5a^2 - 4b^2}{4b^2 - 3a^2} \quad (b)$

36) In $\triangle ABC$ right-angled at C, if $\tan A = 1$, then the value of $2 \sin A \cos A$ is
 (a) 1 (b) $\frac{1}{2}$ (c) 2 (d) $\frac{\sqrt{3}}{2}$

ans:- $\tan A = 1 \Rightarrow A = 45^\circ$

$2 \sin A \cos A = 2 \sin 45^\circ \cos 45^\circ = 2 \times \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} = \frac{2}{2} = 1 \quad (a)$

37) If $\tan \theta = \frac{4}{5}$, then the value of $\frac{5 \sin \theta - 2 \cos \theta}{5 \sin \theta + 2 \cos \theta}$ is

(a) $\frac{1}{3}$ (b) $\frac{2}{5}$ (c) $\frac{3}{5}$ (d) 6

ans:- $\tan \theta = \frac{4}{5} \Rightarrow 5 \tan \theta = 4 \rightarrow (1)$

$\left(\div \cos \theta\right), \frac{5 \tan \theta - 2}{5 \tan \theta + 2} = \frac{4 - 2}{4 + 2} = \frac{2}{6} = \frac{1}{3} \quad (a)$

38) If $\sin \theta = \frac{1}{5}$, then the value of $\frac{1}{5} \cot^2 \theta + \frac{1}{5}$ is (a) $\frac{1}{125}$ (b) $\frac{1}{5}$ (c) 25 (d) 5

ans:- $\sin \theta = \frac{1}{5} \Rightarrow \operatorname{cosec} \theta = 5$

$\therefore \frac{1}{5} (\cot^2 \theta + 1) = \frac{1}{5} \operatorname{cosec}^2 \theta = \frac{1}{5} \times 25 = 5 \quad (d)$

39) If $\cos \theta = \frac{2}{3}$, then $2 \sec^2 \theta + 2 \tan^2 \theta - 7$ is equal to

(a) 1 (b) 0 (c) 3 (d) 4

ans:- $\cos \theta = \frac{2}{3} \Rightarrow \sec \theta = \frac{3}{2}$

$$\begin{aligned} 2 \sec^2 \theta + 2 \tan^2 \theta - 7 &= 2 \sec^2 \theta + 2(\sec^2 \theta - 1) - 7 \\ &= 2 \sec^2 \theta + 2 \sec^2 \theta - 2 - 7 \\ &= 4 \sec^2 \theta - 9 \\ &= 4 \times \frac{9}{4} - 9 \\ &= 9 - 9 = 0 \quad (b) \end{aligned}$$

40) $(\sin 90^\circ - \cos 45^\circ + \cos 60^\circ)(\cos 0^\circ + \sin 45^\circ + \sin 30^\circ) =$
(a) $\frac{5}{8}$ (b) $\frac{7}{4}$ (c) $\frac{4}{7}$ (d) $\frac{3}{5}$

ans:- $(1 - \frac{1}{\sqrt{2}} + \frac{1}{2})(1 + \frac{1}{\sqrt{2}} + \frac{1}{2})$

$$= \left[\left(1 + \frac{1}{2}\right) - \frac{1}{\sqrt{2}} \right] \left[\left(1 + \frac{1}{2}\right) + \frac{1}{\sqrt{2}} \right]$$

$$= \left(\frac{3}{2} - \frac{1}{\sqrt{2}} \right) \left(\frac{3}{2} + \frac{1}{\sqrt{2}} \right) = \left(\frac{3}{2} \right)^2 - \left(\frac{1}{\sqrt{2}} \right)^2$$

$$= \frac{9}{4} - \frac{1 \times 2}{2 \times 2}$$

$$= \frac{9}{4} - \frac{2}{4} = \frac{7}{4} \quad (b)$$