

1. Number System

IX

- 1) Every rational number is
 (a) a natural number (b) an integer
 (c) a real number (d) a whole number.

Soln:- a real number (c)

- 2) Decimal representation of a rational number cannot be
 (a) terminating (b) non-terminating
 (c) non-terminating repeating (d) non-terminating non-repeating

Soln:- The decimal expansion of a rational number is either terminating or non-terminating repeating. So it cannot be non-terminating non-repeating (d)

- 3) π is an irrational number because its decimal expansion is
 (a) terminating (b) non-terminating
 (c) non-terminating repeating (d) non-terminating non-repeating

Soln:- The decimal expansion of an irrational number is non-terminating non-repeating (d)

- 4) Every point on a number line represents
 (a) a unique real number (b) a natural number
 (c) a rational number (d) an irrational number

Soln:- a unique real number (a)

- 5) Which of the following is a rational number?
 (a) $-\frac{2}{3}$ (b) $-\frac{1}{\sqrt{5}}$ (c) $\frac{13}{\sqrt{5}}$ (d) $\frac{\sqrt{2}}{3}$

Soln:- $-\frac{2}{3}$ (a) since $\sqrt{5}$ and $\sqrt{2}$ are irrational numbers.

- 6) Which of the following is irrational?
 (a) 0.15 (b) $0.15\overline{16}$ (c) $0.\overline{1516}$ (d) 0.5015001500015...

Soln:- 0.5015001500015... (d) since the decimal expansion of an irrational number is non-terminating non-repeating

- 7) A rational number equivalent to $\frac{3}{17}$ is
 (a) $\frac{6}{17}$ (b) $\frac{6}{34}$ (c) $\frac{17}{3}$ (d) $\frac{3}{34}$

Soln:- $\frac{3 \times 2}{17 \times 2} = \frac{6}{34}$ (b)

8) A rational number between 2 and 3 is
(a) 2.010010001... (b) $\sqrt{6}$ (c) $\frac{5}{2}$ (d) $4 - \sqrt{2}$

Soln:- $\frac{5}{2} = 2.5$ (c) since all other given numbers are irrational.

9) Four rational numbers between 3 and 4 are
(a) 3.1, 3.2, 3.8, 3.9 (b) $\frac{3}{5}, \frac{4}{5}, 1, \frac{6}{5}$

(c) 3.1, 3.2, 4.1, 4.2 (d) $\frac{13}{5}, \frac{14}{5}, \frac{16}{5}, \frac{17}{5}$

Soln:- 3.1, 3.2, 3.8, 3.9 (a)

10) The smallest irrational number to be added to $3 + \sqrt{2}$ to get a rational number

(a) $-\sqrt{2}$ (b) $3 - \sqrt{2}$ (c) $\sqrt{2} - 3$ (d) $\sqrt{3} + 2$

Soln:- $-\sqrt{2}$ (a). since $3 + \sqrt{2} + (-\sqrt{2}) = 3$, a rational number.

11) Rational number $\frac{3}{40}$ is equal to.

(a) 0.75 (b) 0.12 (c) 0.012 (d) 0.075

Soln:- $\frac{3 \times 25}{40 \times 25} = \frac{75}{1000} = 0.075$ (d)

12) A rational number between 3 and 4 is

(a) $\frac{3}{2}$ (b) $\frac{4}{3}$ (c) $\frac{7}{2}$ (d) $\frac{7}{4}$

Soln:- $\frac{3+4}{2} = \frac{7}{2}$ (c)

13) A rational number between $\frac{3}{5}$ and $\frac{4}{5}$ is

(a) $\frac{1}{5}$ (b) $\frac{7}{10}$ (c) $\frac{3}{10}$ (d) $\frac{4}{10}$

Soln:- $\frac{\frac{3}{5} + \frac{4}{5}}{2} = \frac{1}{2} \times \frac{7}{5} = \frac{7}{10}$ (b)

14) A rational number between $\frac{1}{2}$ and $\frac{3}{4}$ is

(a) $\frac{2}{5}$ (b) $\frac{5}{8}$ (c) $\frac{4}{3}$ (d) $\frac{1}{4}$

Soln:- $\frac{1}{2} \left[\frac{1 \times 2 + 3}{2 \times 2} \right] = \frac{1}{2} \left[\frac{2+3}{4} \right] = \frac{1}{2} \times \frac{5}{4} = \frac{5}{8}$ (b)

15) Which one of the following is not a rational number:
 (a) $\sqrt{2}$ (b) 0 (c) $\sqrt{4}$ (d) $\sqrt{16}$

Soln:- $\sqrt{2}$ (a) since 0, $\sqrt{4}=2$, $\sqrt{16}=4$ are rational numbers.

16) Which one of the following is an irrational number:
 (a) $\sqrt{4}$ (b) $3\sqrt{8}$ (c) $\sqrt{100}$ (d) $-\sqrt{0.64}$

Soln:- $3\sqrt{8} = 3 \times 2\sqrt{2} = 6\sqrt{2}$ (b) since $\sqrt{4}=2$, $\sqrt{100}=10$, $-\sqrt{0.64}=-0.8$ are rational numbers.

17) Decimal representation of $\frac{1}{5}$ is:
 (a) 0.2 (b) 0.5 (c) 0.02 (d) 0.002

Soln:- $\frac{1 \times 2}{5 \times 2} = \frac{2}{10} = 0.2$ (a)

18) $3\frac{3}{8}$ in decimal form is:
 (a) 3.35 (b) 3.375 (c) 33.75 (d) 337.5

Soln:- $3\frac{3}{8} = \frac{27 \times 125}{8 \times 125} = \frac{3375}{1000} = 3.375$ (b)

19) $\frac{5}{6}$ in the decimal form is:
 (a) $0.8\bar{3}$ (b) $0.8\bar{33}$ (c) $0.6\bar{3}$ (d) $0.6\bar{33}$

Soln:- $\frac{1}{6} = 0.1\bar{6}$

$\therefore \frac{5}{6} = 5 \times 0.1\bar{6} = 0.8\bar{3}$ (a)

20) Decimal representation of rational number $\frac{8}{27}$ is:
 (a) $0.29\bar{6}$ (b) $0.29\bar{6}$ (c) $0.2\bar{96}$ (d) 0.296

Soln:- $\frac{8}{27} = 0.29\bar{6}$ (a)

$$\begin{array}{r} 0.296296\dots \\ 27 \overline{) 80} \\ \underline{54} \\ 260 \\ \underline{243} \\ 170 \\ \underline{162} \\ 80 \end{array}$$

21) Which one of the following is a rational number: (a) $\sqrt{3}$ (b) $\sqrt{2}$ (c) 0 (d) $\sqrt{5}$

Soln:- 0 (c) since 0 can be written in the form $\frac{p}{q}$, $q \neq 0$
 eg: $-\frac{0}{1}$, $\frac{0}{2}$ etc.

22) $0.6666\dots$ in $\frac{p}{q}$ form is:

- (a) $\frac{6}{99}$ (b) $\frac{2}{3}$ (c) $\frac{3}{5}$ (d) $\frac{1}{66}$

Soln:- Let $x = 0.\overline{6666\dots} \rightarrow (1)$

$$10x = 6.6666\dots \rightarrow (2)$$

$$(2) - (1), 9x = 6$$

$$x = \frac{6}{9} = \frac{2}{3} \quad (b)$$

23) The value of $0.\overline{3}$ in the form $\frac{p}{q}$, where p and q are integers and $q \neq 0$ is

- (a) $\frac{33}{100}$ (b) $\frac{3}{10}$ (c) $\frac{1}{3}$ (d) $\frac{3}{100}$

Soln:- Let $x = 0.\overline{3333\dots} \rightarrow (1)$

$$10x = 3.3333\dots \rightarrow (2)$$

$$(2) - (1), 9x = 3$$

$$x = \frac{3}{9} = \frac{1}{3} \quad (c)$$

24) $0.3\overline{2}$ expressed in the form $\frac{p}{q}$, where p and q are integers and $q \neq 0$ is

- (a) $\frac{8}{25}$ (b) $\frac{29}{90}$ (c) $\frac{32}{99}$ (d) $\frac{32}{199}$

Soln:- Let $x = 0.3\overline{2222\dots} \rightarrow (1)$

$$10x = 3.\overline{2222\dots} \rightarrow (1)$$

$$100x = 32.\overline{2222\dots} \rightarrow (2)$$

$$90x = 29$$

$$x = \frac{29}{90} \quad (b)$$

25) $0.\overline{437}$ expressed in the form $\frac{p}{q}$, where p and q are integers and $q \neq 0$ is

- (a) $\frac{437}{9999}$ (b) $\frac{394}{999}$ (c) $\frac{434}{99}$ (d) $\frac{437}{999}$

Soln:- Let $x = 0.\overline{437437437\dots} \rightarrow (1)$

$$1000x = 437.\overline{437437437\dots} \rightarrow (2)$$

$$(2) - (1), 999x = 437$$

$$x = \frac{437}{999} \quad (d)$$

26) Simplest rationalisation factor of $\sqrt[3]{40}$ is

- (a) $\sqrt[3]{25}$ (b) $\sqrt[3]{5}$ (c) $\sqrt{40}$ (d) $\sqrt{5}$

Soln:-

$$\sqrt[3]{40} = \sqrt[3]{2 \times 2 \times 2 \times 5}$$

\therefore the rationalisation factor = $\sqrt[3]{25}$

since the factor 5 is not in triplets

$$\begin{array}{r} 2 \overline{)40} \\ \underline{20} \\ 20 \\ \underline{20} \\ 0 \end{array}$$

27) $2\sqrt{5} + \sqrt{5}$ equals (a) $2\sqrt{10}$ (b) 10 (c) $3\sqrt{5}$ (d) $3\sqrt{10}$

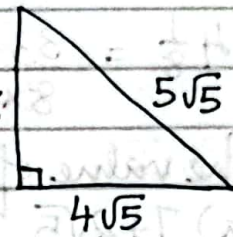
Soln:-

$3\sqrt{5}$ (c)

28) The perimeter of the given figure is

- (a) $60\sqrt{5}$ (b) $12\sqrt{5}$ (c) $27\sqrt{5}$ (d) $32\sqrt{5}$

$3\sqrt{5}$



Soln:-

perimeter = $3\sqrt{5} + 4\sqrt{5} + 5\sqrt{5}$

= $12\sqrt{5}$ (b)

29) On simplification of $\left(\frac{2\sqrt{5}-1\sqrt{2}+6\sqrt{11}}{3}\right) + \left(\frac{1\sqrt{5}+\frac{3}{2}\sqrt{2}-\sqrt{11}}{2}\right)$, we get

- (a) $\sqrt{5} + \sqrt{2} + 5\sqrt{11}$ (b) $\frac{\sqrt{5}}{2} + 2\sqrt{2} + \sqrt{11}$ (c) $\sqrt{5} + \sqrt{2} + 6\sqrt{11}$ (d) $\sqrt{5} + 2\sqrt{2} + 5\sqrt{11}$

Soln:-

$$\sqrt{5} \left(\frac{2}{3} + \frac{1}{3}\right) + \sqrt{2} \left(\frac{3}{2} - \frac{1}{2}\right) + \sqrt{11} (6 - 1)$$

$$= \sqrt{5} \times \frac{3}{3} + \sqrt{2} \times \frac{2}{2} + \sqrt{11} \times 5 = \sqrt{5} + \sqrt{2} + 5\sqrt{11} \text{ (a)}$$

30) The product of $\sqrt[3]{7}$ and $\sqrt{5}$ is

- (a) $\sqrt[3]{35}$ (b) $\sqrt[6]{35}$ (c) $\sqrt[6]{6125}$ (d) $\sqrt[6]{1225}$

Soln:-

$$\sqrt[3]{7} \times \sqrt{5} = 7^{\frac{1 \times 2}{3}} \times 5^{\frac{1 \times 3}{2}}$$

$$= 7^{\frac{2}{3}} \times 5^{\frac{3}{2}} = (7^2)^{\frac{1}{3}} \times (5^3)^{\frac{1}{2}} = (7^2 \times 5^3)^{\frac{1}{6}}$$

$$= (49 \times 125)^{\frac{1}{6}} = (6125)^{\frac{1}{6}} = \sqrt[6]{6125} \text{ (c)}$$

31) The product of $\frac{1}{6}\sqrt{18}$ and $\frac{1}{3}\sqrt{18}$ is

- (a) 1 (b) $\frac{1}{12}$ (c) $\frac{1}{3}$ (d) $\sqrt{2}$

Soln:-

$$\frac{1}{6}\sqrt{18} \times \frac{1}{3}\sqrt{18} = \frac{1}{6} \times \frac{1}{3} \times \sqrt{18} \times \sqrt{18} = \frac{1}{18} \times 18 = 1 \text{ (a)}$$

32) $\sqrt{5} \times \sqrt{7} \times \sqrt{15} \times \sqrt{21}$ in simplified form is

- (a) $\sqrt{105}$ (b) $\sqrt{210}$ (c) 105 (d) 210

Soln:-

$$\sqrt{5} \times \sqrt{7} \times \sqrt{3} \times \sqrt{5} \times \sqrt{7} \times \sqrt{3} = 5 \times 7 \times 3 = 105 \text{ (c)}$$

33) $(3+\sqrt{3})(3-\sqrt{3})$ on simplification becomes equal to
(a) 18 (b) $2\sqrt{3}$ (c) 6 (d) 9

Soln:- $(3+\sqrt{3})(3-\sqrt{3}) = (3)^2 - (\sqrt{3})^2$ $[(a+b)(a-b) = a^2 - b^2]$
 $= 9 - 3 = 6$ (c)

34) $4\frac{1}{8}$ in decimal form is:

(a) 4.125 (b) $4.\overline{15}$ (c) $4.1\overline{5}$ (d) $0.4\overline{15}$

Soln:-

$$4\frac{1}{8} = \frac{33 \times 125}{8 \times 125} = \frac{4125}{1000} = 4.125$$
 (a)

35) The value of $(\sqrt{5}+\sqrt{2})^2$ is:

(a) $7+2\sqrt{5}$ (b) $1+5\sqrt{2}$ (c) $7+2\sqrt{10}$ (d) $7-2\sqrt{10}$

Soln:- $(\sqrt{5}+\sqrt{2})^2 = 5+2+2\sqrt{10}$ $[(a+b)^2 = a^2 + b^2 + 2ab]$
 $= 7+2\sqrt{10}$ (c)

36) The value of $(\sqrt{5}+\sqrt{2})(\sqrt{5}-\sqrt{2})$ is:

(a) 10 (b) 7 (c) 3 (d) $\sqrt{3}$

Soln:- $(\sqrt{5}+\sqrt{2})(\sqrt{5}-\sqrt{2}) = (\sqrt{5})^2 - (\sqrt{2})^2 = 5 - 2 = 3$ (c)

37) The value of $(3+\sqrt{3})(2+\sqrt{2})$ is:

(a) $6+3\sqrt{2}+2\sqrt{3}+\sqrt{6}$ (b) $3+3\sqrt{2}+3\sqrt{3}+6$
(c) $6-3\sqrt{2}-2\sqrt{3}-\sqrt{6}$ (d) $6-3\sqrt{2}+2\sqrt{3}-\sqrt{6}$

Soln:- $(3+\sqrt{3})(2+\sqrt{2}) = 6+3\sqrt{2}+2\sqrt{3}+\sqrt{6}$ (a)

38) The value of $(\sqrt{11}+\sqrt{7})(\sqrt{11}-\sqrt{7})$ is:

(a) 4 (b) -4 (c) 18 (d) -18

Soln:- $(\sqrt{11}+\sqrt{7})(\sqrt{11}-\sqrt{7}) = (\sqrt{11})^2 - (\sqrt{7})^2$
 $= 11 - 7 = 4$ (a)

39) The value of $(5+\sqrt{5})(5-\sqrt{5})$ is:

(a) 0 (b) 25 (c) 20 (d) -20

Soln:- $(5+\sqrt{5})(5-\sqrt{5}) = (5)^2 - (\sqrt{5})^2 = 25 - 5 = 20$ (c)

40) On rationalizing the denominator of $\frac{1}{\sqrt{7}}$, we get

(a) 7 (b) $\frac{\sqrt{7}}{7}$ (c) $-\frac{\sqrt{7}}{7}$ (d) $\sqrt{7}$

Soln:- $\frac{1 \times \sqrt{7}}{\sqrt{7} \times \sqrt{7}} = \frac{\sqrt{7}}{7}$ (b)

41) On rationalizing the denominator of $\frac{1}{\sqrt{7}-\sqrt{6}}$, we get

(a) $\frac{\sqrt{7}+\sqrt{6}}{\sqrt{7}-\sqrt{6}}$ (b) $\frac{\sqrt{7}-\sqrt{6}}{\sqrt{7}+\sqrt{6}}$ (c) $\sqrt{7}+\sqrt{6}$ (d) $\sqrt{7}-\sqrt{6}$

Soln:- $\frac{1(\sqrt{7}+\sqrt{6})}{(\sqrt{7}-\sqrt{6})(\sqrt{7}+\sqrt{6})} = \frac{\sqrt{7}+\sqrt{6}}{(\sqrt{7})^2 - (\sqrt{6})^2} = \frac{\sqrt{7}+\sqrt{6}}{7-6} = \sqrt{7}+\sqrt{6}$ (c)

42) On rationalizing the denominator of $\frac{1}{\sqrt{5}+\sqrt{2}}$, we get

(a) $\sqrt{5}-\sqrt{2}$ (b) $\sqrt{2}-\sqrt{5}$ (c) $\frac{\sqrt{5}-\sqrt{2}}{3}$ (d) $\frac{\sqrt{2}-\sqrt{5}}{3}$

Soln:- $\frac{1(\sqrt{5}-\sqrt{2})}{(\sqrt{5}+\sqrt{2})(\sqrt{5}-\sqrt{2})} = \frac{\sqrt{5}-\sqrt{2}}{(\sqrt{5})^2 - (\sqrt{2})^2} = \frac{\sqrt{5}-\sqrt{2}}{5-2} = \frac{\sqrt{5}-\sqrt{2}}{3}$ (c)

43) On rationalizing the denominator of $\frac{1}{\sqrt{7}-2}$, we get

(a) $\sqrt{7}-2$ (b) $\sqrt{7}+2$ (c) $\frac{\sqrt{7}+2}{3}$ (d) $\frac{\sqrt{7}-2}{3}$

Soln:- $\frac{1(\sqrt{7}+2)}{(\sqrt{7}-2)(\sqrt{7}+2)} = \frac{\sqrt{7}+2}{(\sqrt{7})^2 - (2)^2} = \frac{\sqrt{7}+2}{7-4} = \frac{\sqrt{7}+2}{3}$ (c)

44) The value of $(3+\sqrt{5})^2(3-\sqrt{5})^2$ is

(a) 15 (b) 16 (c) 4 (d) 14

Soln:- $(3+\sqrt{5})^2(3-\sqrt{5})^2 = [(3+\sqrt{5})(3-\sqrt{5})]^2$
 $= [3^2 - (\sqrt{5})^2]^2$
 $= (9-5)^2 = 4^2 = 16$ (b)

45) $\sqrt[3]{250} \div \sqrt[3]{10}$ in simplified form is equal to

(a) $\sqrt[3]{25}$ (b) 5 (c) $\sqrt{5}$ (d) $\sqrt[3]{2500}$

Soln:- $\frac{\sqrt[3]{250}}{\sqrt[3]{10}} = \sqrt[3]{\frac{250}{10}} = \sqrt[3]{25}$ (a)

46) $\frac{30}{\sqrt{20}+\sqrt{5}}$ is equal to (a) $\frac{10}{3\sqrt{5}}$ (b) $\frac{30}{\sqrt{5}}$ (c) $\frac{10}{\sqrt{5}}$ (d) $12\sqrt{5}$

Soln:- $\frac{30}{\sqrt{20}+\sqrt{5}} = \frac{30}{2\sqrt{5}+\sqrt{5}} = \frac{30}{3\sqrt{5}}$
 $= \frac{10}{\sqrt{5}}$ (c)

47) $\frac{6}{\sqrt{2}-\sqrt{3}}$ is equal to (a) $\frac{1}{\sqrt{3}}$ (b) $\frac{2}{\sqrt{3}}$ (c) $2\sqrt{3}$ (d) $6\sqrt{3}$

Soln:- $\frac{6}{\sqrt{2}-\sqrt{3}} = \frac{6}{2\sqrt{3}-\sqrt{3}} = \frac{6 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} = \frac{2 \times 12}{3} = \frac{24}{3} = 8$
 $= \frac{2 \times 6\sqrt{3}}{3} = 2\sqrt{3}$ (c)

48) The value of $\frac{2^0+7^0}{5^0}$ is (a) 2 (b) 0 (c) $\frac{9}{5}$ (d) $\frac{1}{5}$

Soln:- $\frac{2^0+7^0}{5^0} = \frac{1+1}{1} = 2$ (a) [a⁰=1]

49) On simplifying $\frac{2^{30}+2^{29}}{2^{31}-2^{30}}$, we get:

(a) 1 (b) 2 (c) $\frac{2}{3}$ (d) $\frac{3}{2}$

Soln:- $\frac{2^{29}(2^1+1)}{2^{29}(2^2-2^1)} = \frac{2+1}{4-2} = \frac{3}{2}$ (d)

50) The value of $\sqrt{3^{-2}}$ is (a) $\frac{1}{9}$ (b) 9 (c) -3 (d) $\frac{1}{3}$

Soln:- $\sqrt{3^{-2}} = \sqrt{\frac{1}{3^2}} = \sqrt{\frac{1}{9}} = \frac{1}{3}$ (d)

51) $\left(\frac{256}{625}\right)^{-\frac{3}{4}}$ in its simplified form is equal to

(a) $\frac{25}{64}$ (b) $\frac{64}{125}$ (c) $\frac{125}{64}$ (d) $\frac{64}{25}$

Soln:- $\left(\frac{256}{625}\right)^{-\frac{3}{4}} = \left(\frac{4^4}{5^4}\right)^{-\frac{3}{4}} = \frac{4^{4 \times -\frac{3}{4}}}{5^{4 \times -\frac{3}{4}}} = \frac{4^{-3}}{5^{-3}} = \frac{5^3}{4^3} = \frac{125}{64}$ (c)

52) $(32)^{\frac{1}{3}} \times (125)^{-\frac{1}{3}}$ in its simplified form is
 (a) $\frac{16}{25}$ (b) $\frac{4}{5}$ (c) $\frac{2}{5}$ (d) $\frac{2}{25}$

Soln:- $(32)^{\frac{1}{5}} \times (125)^{-\frac{1}{3}} = 2^{5 \times \frac{1}{5}} \times 5^{3 \times -\frac{1}{3}}$
 $= 2 \times 5 = \frac{2}{5}$ (c)

53) $\frac{5^{n+2} - 6 \cdot 5^{n+1}}{13 \cdot 5^n - 2 \cdot 5^{n+1}} =$ (a) $\frac{5}{3}$ (b) $-\frac{5}{3}$ (c) $\frac{3}{5}$ (d) $-\frac{3}{5}$

Soln:- $\frac{5^n \cdot 5^2 - 6 \cdot 5^n \cdot 5}{13 \cdot 5^n - 2 \cdot 5^n \cdot 5} = \frac{5^n (5^2 - 6 \times 5)}{5^n (13 - 2 \times 5)} = \frac{25 - 30}{13 - 10}$
 $= -\frac{5}{3}$ (b)

54) On rationalizing the denominator of $\frac{1}{\sqrt{2}}$, we get
 (a) 2 (b) $\sqrt{2}$ (c) $\frac{2}{\sqrt{2}}$ (d) $\frac{\sqrt{2}}{2}$

Soln:- $\frac{1 \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} = \frac{\sqrt{2}}{2}$ (d)

55) On rationalizing the denominator of $\frac{1}{2+\sqrt{3}}$, we get

(a) $2-\sqrt{3}$ (b) $\sqrt{3}-2$ (c) $2+\sqrt{3}$ (d) $-\sqrt{3}-2$

Soln:- $\frac{1(2-\sqrt{3})}{(2+\sqrt{3})(2-\sqrt{3})} = \frac{2-\sqrt{3}}{(2)^2 - (\sqrt{3})^2} = \frac{2-\sqrt{3}}{4-3} = \frac{2-\sqrt{3}}{1}$ (a)

56) On rationalizing the denominator of $\frac{1}{\sqrt{3}-\sqrt{2}}$, we get

(a) $\frac{1}{\sqrt{3}+\sqrt{2}}$ (b) $\sqrt{3}+\sqrt{2}$ (c) $\sqrt{2}-\sqrt{3}$ (d) $-\sqrt{3}-\sqrt{2}$

Soln:- $\frac{1 \cdot (\sqrt{3}+\sqrt{2})}{(\sqrt{3}-\sqrt{2})(\sqrt{3}+\sqrt{2})} = \frac{\sqrt{3}+\sqrt{2}}{(\sqrt{3})^2 - (\sqrt{2})^2} = \frac{\sqrt{3}+\sqrt{2}}{3-2} = \frac{\sqrt{3}+\sqrt{2}}{1} = \sqrt{3}+\sqrt{2}$ (b)

57) The value of $64^{\frac{1}{2}}$ is (a) 8 (b) 4 (c) 16 (d) 32

Soln:- $64^{\frac{1}{2}} = 8^{2 \times \frac{1}{2}} = 8$ (a)

58) The value of $32^{\frac{1}{5}}$ is (a) 16 (b) 160 (c) 2 (d) 18

Soln:- $32^{\frac{1}{5}} = 2^{5 \times \frac{1}{5}} = 2$ (c)

59) The value of $(125)^{\frac{1}{3}}$ is
 (a) 5 (b) 25 (c) 45 (d) 35

Soln:-
 $(125)^{\frac{1}{3}} = 5^{3 \times \frac{1}{3}} = 5$ (a)

60) The value of $9^{\frac{3}{2}}$ is
 (a) 18 (b) 27 (c) -18 (d) $\frac{1}{27}$

Soln:-
 $9^{\frac{3}{2}} = 3^{2 \times \frac{3}{2}} = 3^3 = 27$ (b)

61) The value of $32^{\frac{2}{5}}$ is:
 (a) 2 (b) 4 (c) 16 (d) 14

Soln:-
 $32^{\frac{2}{5}} = 2^{5 \times \frac{2}{5}} = 2^2 = 4$ (b)

62) The value of $16^{\frac{3}{4}}$ is
 (a) 4 (b) 12 (c) 8 (d) 48

Soln:-
 $16^{\frac{3}{4}} = 2^{4 \times \frac{3}{4}} = 2^3 = 8$ (c)

63) The value of $125^{-\frac{1}{3}}$ is
 (a) $\frac{1}{5}$ (b) $\frac{1}{25}$ (c) $\frac{1}{15}$ (d) $\frac{1}{125}$

Soln:-
 $125^{-\frac{1}{3}} = 5^{3 \times -\frac{1}{3}} = 5^{-1} = \frac{1}{5}$ (a)

64) The value of $11^{\frac{1}{2}} \div 11^{\frac{1}{4}}$ is
 (a) $11^{\frac{1}{4}}$ (b) $11^{\frac{3}{4}}$ (c) $11^{\frac{1}{8}}$ (d) $11^{\frac{1}{2}}$

Soln:-
 $11^{\frac{1}{2}} \div 11^{\frac{1}{4}} = 11^{\frac{1 \times 2}{2 \times 2} - \frac{1}{4}} = 11^{\frac{2-1}{4}} = 11^{\frac{1}{4}}$ (a)

65) The value of $64^{-\frac{3}{2}}$ is
 (a) $\frac{1}{96}$ (b) $\frac{1}{64}$ (c) 512 (d) $\frac{1}{512}$

Soln:-
 $64^{-\frac{3}{2}} = 8^{2 \times -\frac{3}{2}} = 8^{-3} = \frac{1}{8^3} = \frac{1}{512}$ (d)

66) The value of $125^{\frac{2}{3}}$ is
 (a) 5 (b) 25 (c) 45 (d) 35

Soln:-
 $125^{\frac{2}{3}} = 5^{3 \times \frac{2}{3}} = 5^2 = 25$ (b)

67) The value of $\left[8^{-\frac{4}{3}} \div 2^{-2}\right]^{\frac{1}{2}}$ is
 (a) $\frac{1}{2}$ (b) 2 (c) $\frac{1}{4}$ (d) 4

Soln:- $\left[2^{3 \times \frac{-4}{3}} \div 2^{-2}\right]^{\frac{1}{2}} = \left[2^{-4} \div 2^{-2}\right]^{\frac{1}{2}} = \left[2^{-4+2}\right]^{\frac{1}{2}}$
 $= \left(2^{-2}\right)^{\frac{1}{2}} = 2^{-1} = \frac{1}{2}$ (a)

68) If x is a positive real number, then $\sqrt[4]{\sqrt[3]{x^2}}$ is
 (a) $x^{\frac{1}{24}}$ (b) $x^{\frac{1}{6}}$ (c) $x^{\frac{1}{12}}$ (d) $x^{\frac{1}{20}}$

Soln:- $x^{2 \times \frac{1}{3} \times \frac{1}{4}} = x^{\frac{1}{6}}$ (b)

69) If $x=2$ and $y=3$, then the value of $x^y + y^x$ is
 (a) 15 (b) 17 (c) 19 (d) 21

Soln:- $2^3 + 3^2 = 8 + 9 = 17$ (b)

70) If $x = 9 - 4\sqrt{5}$, then $x + \frac{1}{x}$ is equal to

(a) $8\sqrt{5}$ (b) $-8\sqrt{5}$ (c) 18 (d) 81

Soln:- $x = 9 - 4\sqrt{5}$
 $\frac{1}{x} = \frac{1}{9 - 4\sqrt{5}} = \frac{9 + 4\sqrt{5}}{9^2 - (4\sqrt{5})^2} = \frac{9 + 4\sqrt{5}}{81 - 80}$

$\therefore x + \frac{1}{x} = 9 - 4\sqrt{5} + 9 + 4\sqrt{5} = 18$

71) Which of the following is equal to a ?

(a) $a^{\frac{13}{7} - \frac{5}{7}}$ (b) $\sqrt[12]{(a^4)^{\frac{1}{3}}}$ (c) $(\sqrt{a^5})^{\frac{2}{5}}$ (d) $a^{\frac{13}{7}} \times a^{\frac{7}{13}}$

Soln:- $(\sqrt{a^5})^{\frac{2}{5}} = \left(a^{\frac{5}{2}}\right)^{\frac{2}{5}} = a^{\frac{5}{2} \times \frac{2}{5}} = a$ (c)

72) Decimal representation of $-\frac{17}{8}$ is

(a) -2.125 (b) -2.225 (c) 2.125 (d) -1.175

Soln:- $\frac{-17 \times 125}{8 \times 125} = \frac{-2125}{1000} = -2.125$ (a)

73) If $\frac{3}{7} = 0.\overline{428571}$, then $\frac{5}{7}$ is equal to

- (a) $0.\overline{704125}$ (b) $0.\overline{714285}$ (c) $0.\overline{77132}$ (d) $0.\overline{714381}$

Soln:-

$$\frac{1}{7} = 0.\overline{142857}$$

$$\frac{5}{7} = 5 \times 0.\overline{142857} = 0.\overline{714285} \text{ (b)}$$

74) If $\sqrt{3} = 1.732$, then the value of $\frac{1}{\sqrt{3}}$ approximately is

- (a) 0.866 (b) 0.433 (c) 0.288 (d) 0.577

Soln:-

$$\frac{1 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} = \frac{\sqrt{3}}{3} = \frac{1.732}{3} \approx 0.577 \text{ (d)}$$

75) If $\sqrt{2} = 1.414$, then the value of $\sqrt{3} \div \sqrt{6}$ upto three places of decimal is

- (a) 0.235 (b) 0.707 (c) 1.414 (d) 0.471

Soln:-

$$\frac{\sqrt{3}}{\sqrt{6}} = \frac{\sqrt{3}}{\sqrt{2} \times \sqrt{3}} = \frac{1 \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} = \frac{\sqrt{2}}{2} = \frac{1.414}{2} = 0.707 \text{ (b)}$$

76) The value of $25^{3/2}$ is

- (a) 5 (b) 25 (c) 125 (d) 625

Soln:-

$$25^{3/2} = 5^{2 \times \frac{3}{2}} = 5^3 = 125 \text{ (c)}$$

77) The value of $\frac{1}{11}$ in decimal form is:

- (a) $0.0\overline{99}$ (b) $0.\overline{909}$ (c) $0.\overline{09}$ (d) $0.00\overline{9}$

Soln:-

$$\frac{1}{11} = 0.\overline{09} \text{ (c)}$$

78) Decimal expansion of a rational number is terminating if in its denominator there is:

- (a) 2 or 5 (b) 3 or 5 (c) 9 or 11 (d) 3 or 7

Soln:-

$$2 \text{ or } 5 \text{ (a)}$$

79) The exponent form of $\sqrt[3]{7}$ is

- (a) 7^3 (b) 3^7 (c) $7^{1/3}$ (d) $3^{1/7}$

Soln:-

$$7^{1/3} \text{ (c)}$$

80) Which of the following is true?

- (a) Every whole number is a natural number
- (b) Every integer is a rational number
- (c) Every rational number is an integer
- (d) Every integer is a whole number

Soln:- Every integer is a rational number (b)

81) For positive real numbers a and b , which is not true?

- (a) $\sqrt{ab} = \sqrt{a}\sqrt{b}$
- (b) $(a+\sqrt{b})(a-\sqrt{b}) = a^2 - b$
- (c) $\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$
- (d) $(\sqrt{a}+\sqrt{b})(\sqrt{a}-\sqrt{b}) = a+b$

Soln:- $(\sqrt{a}+\sqrt{b})(\sqrt{a}-\sqrt{b}) = (\sqrt{a})^2 - (\sqrt{b})^2 = a - b \neq a + b$ (d)

82) Out of the following, the irrational number is

- (a) $1.\bar{5}$
- (b) $2.4\bar{77}$
- (c) $1.2\bar{77}$
- (d) π

Soln:- π (d)

83) To rationalize the denominator of $\frac{1}{\sqrt{a}+b}$, we multiply this by

- (a) $\frac{1}{\sqrt{a}+b}$
- (b) $\frac{1}{\sqrt{a}-b}$
- (c) $\frac{\sqrt{a}+b}{\sqrt{a}+b}$
- (d) $\frac{\sqrt{a}-b}{\sqrt{a}-b}$

Soln:- $\frac{1(\sqrt{a}-b)}{(\sqrt{a}+b)(\sqrt{a}-b)}$ (d)

84) The number of rational numbers between $\sqrt{3}$ and $\sqrt{5}$ is

- (a) one
- (b) 3
- (c) none
- (d) infinitely many

Soln:- infinitely many (d)

85) If we add two irrational numbers, the resulting number

- (a) is always an irrational number
- (b) is always a rational no.
- (c) may be a rational or an irrational no.
- (d) always an integer

Soln:- may be a rational or an irrational number (c)

86) The rationalizing factor of $7-2\sqrt{3}$ is

- (a) $7-2\sqrt{3}$
- (b) $7+2\sqrt{3}$
- (c) $5+2\sqrt{3}$
- (d) $4+2\sqrt{3}$

Soln:- $(7-2\sqrt{3})(7+2\sqrt{3})$ (b)

87) If $\frac{1}{7} = 0.\overline{142857}$, then $\frac{4}{7}$ equals

- (a) $0.\overline{428571}$
- (b) $0.\overline{571428}$
- (c) $0.\overline{857142}$
- (d) $0.\overline{285718}$

Soln:- $\frac{4}{7} = 4 \times 0.\overline{142857} = 0.\overline{571428}$ (b)

88) The value of n for which \sqrt{n} be a rational number is (a) 2 (b) 4 (c) 3 (d) 5

Soln:- $\sqrt{4} = 2$, a rational number (b).

89) $\frac{3\sqrt{12}}{6\sqrt{27}}$ equals (a) $\frac{1}{2}$ (b) $\sqrt{2}$ (c) $\sqrt{3}$ (d) $\frac{1}{3}$

Soln:- $\frac{3 \times 2\sqrt{3}}{6 \times 3\sqrt{3}} = \frac{2}{6} = \frac{1}{3}$ (d)

90) $(3 + \sqrt{3})(3 - \sqrt{2})$ equals (a) $9 - 5\sqrt{2} - \sqrt{6}$ (b) $9 - \sqrt{6}$ (c) $3 + \sqrt{2}$ (d) $9 - 3\sqrt{2} + 3\sqrt{3} - \sqrt{6}$

Soln:- $(3 + \sqrt{3})(3 - \sqrt{2}) = 9 - 3\sqrt{2} + 3\sqrt{3} - \sqrt{6}$ (d)

91) The arrangement of $\sqrt{5}, \sqrt{2}, \sqrt{3}$ in ascending order is (a) $\sqrt{2}, \sqrt{3}, \sqrt{5}$ (b) $\sqrt{2}, \sqrt{5}, \sqrt{3}$ (c) $\sqrt{5}, \sqrt{3}, \sqrt{2}$ (d) $\sqrt{3}, \sqrt{2}, \sqrt{5}$

Soln:- $\sqrt{5} = 2.236$

$\sqrt{2} = 1.414$

$\sqrt{3} = 1.732$

$\therefore \sqrt{2} < \sqrt{3} < \sqrt{5}$ (a)

92) If m and n are two natural numbers and $m^n = 32$, then n^{mn} is

(a) 5^2 (b) 5^3 (c) 5^{10} (d) 5^{12}

Soln:-

$$2^5 = 32$$

$$\therefore m = 2, n = 5$$

$$\text{Thus, } n^{mn} = 5^{2 \times 5} = 5^{10} \text{ (c)}$$

93) If $\sqrt{10} = 3.162$, then value of $\frac{1}{\sqrt{10}}$ is

(a) 0.3162 (b) 3.162 (c) 31.62 (d) 316.2

Soln:-

$$\frac{1 \times \sqrt{10}}{\sqrt{10} \times \sqrt{10}} = \frac{\sqrt{10}}{10} = \frac{3.162}{10} = 0.3162 \text{ (a)}$$

94) Find the value of $(1296)^{0.17} \times (1296)^{0.08}$

(a) 2 (b) 4 (c) 3 (d) 6

Soln:-

$$(1296)^{0.17+0.08} = (1296)^{0.25} = (1296)^{\frac{1}{4}} = 6^{\frac{4 \times 1}{4}} = 6 \text{ (d)}$$

95) If $(3^3)^2 = 9^x$, then $5^x = ?$
 (a) 1 (b) 5 (c) 25 (d) 125

Soln:-

$$(3^2)^3 = (3^2)^x$$

$$\therefore x = 3$$

$$\text{Then, } 5^x = 5^3 = 125 \text{ (d)}$$

96)

$$\sqrt[3]{2} \times \sqrt[4]{2} \times \sqrt[12]{32} = ?$$

(a) 2 (b) $\sqrt{2}$ (c) $2\sqrt{2}$ (d) $4\sqrt{2}$

Soln:-

$$2^{\frac{1}{3}} \times 2^{\frac{1}{4}} \times (2^5)^{\frac{1}{12}} = 2^{\frac{1 \times 4}{3 \times 4} + \frac{1 \times 3}{4 \times 3} + \frac{5}{12}}$$

$$= 2^{\frac{4+3+5}{12}} = 2^{\frac{12}{12}} = 2 \text{ (a)}$$

97) If $\left(\frac{2}{3}\right)^x \times \left(\frac{3}{2}\right)^{2x} = \frac{81}{16}$, then the value of x is

(a) 1 (b) 2 (c) 3 (d) 4

Soln:-

$$\left(\frac{2}{3}\right)^x \times \left(\frac{2}{3}\right)^{-2x} = \frac{81}{16}$$

$$\left(\frac{2}{3}\right)^{x-2x} = \frac{81}{16}$$

$$\left(\frac{2}{3}\right)^{-x} = \frac{3^4}{2^4} = \left(\frac{3}{2}\right)^4$$

$$\left(\frac{2}{3}\right)^{-x} = \left(\frac{2}{3}\right)^{-4}$$

$$\therefore -x = -4$$

$$x = 4 \text{ (d)}$$

98) The value of $x^{p-q} \cdot x^{q-r} \cdot x^{r-p}$ is equal to

(a) 0 (b) 1 (c) x (d) x^{pqr}

Soln:-

$$x^{p-q+q-r+r-p} = x^0 = 1 \text{ (b)}$$

99) If $\left(\frac{3}{4}\right)^6 \times \left(\frac{16}{9}\right)^5 = \left(\frac{4}{3}\right)^{x+2}$, then the value of x is

(a) 2 (b) 4 (c) -2 (d) 6

Soln:- $\left(\frac{3}{4}\right)^6 \times \left(\frac{9}{16}\right)^{-5} = \left(\frac{3}{4}\right)^{-x-2}$

$\left(\frac{3}{4}\right)^6 \times \left(\frac{3}{4}\right)^{-10} = \left(\frac{3}{4}\right)^{-x-2}$

$\left(\frac{3}{4}\right)^{6-10} = \left(\frac{3}{4}\right)^{-x-2}$

$\therefore -4 = -x - 2$

$-4 + 2 = -x$

$-x = -2$

$\therefore x = 2$ (a)

100) The value of $\frac{\sqrt{2}-1}{\sqrt{2}+1} =$ (a) 2.4142... (b) 5.8282...
 if $\sqrt{2} = 1.4142...$ (c) 0.4142... (d) 0.1718...

Soln:-

$\frac{(\sqrt{2}-1)^2}{(\sqrt{2})^2-1^2} = \frac{(\sqrt{2}-1)^2}{2-1} = \sqrt{2}-1$
 $= 1.4142... - 1$
 $= 0.4142... (c)$

101) The value of $\frac{\sqrt{32} + \sqrt{48}}{\sqrt{8} + \sqrt{12}} =$

(a) $\sqrt{2}$ (b) 2 (c) 4 (d) 8

Soln:-

$\frac{4\sqrt{2} + 4\sqrt{3}}{2\sqrt{2} + 2\sqrt{3}} = \frac{4(\sqrt{2} + \sqrt{3})}{2(\sqrt{2} + \sqrt{3})} = \frac{4}{2} = 2$ (b)

102) The value of 1.999... in the form $\frac{p}{q}$; $q \neq 0$
 (a) $\frac{19}{10}$ (b) $\frac{1999}{1000}$ (c) 2 (d) $\frac{1}{9}$

Soln:- 2 (c)

103) A rational number between $\sqrt{2}$ and $\sqrt{3}$ is
 (a) $\frac{\sqrt{2} + \sqrt{3}}{2}$ (b) $\sqrt{2} \cdot \sqrt{3}$ (c) 1.5 (d) 1.8

Soln:- $\sqrt{2} = 1.414$; $\sqrt{3} = 1.732$ $\therefore 1.5$ (c)